Dyscalculia and Typical Math Achievement Are Associated With Individual Differences in Number-Specific Executive Function

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Deficits in numerical magnitude perception characterize the mathematics learning disability developmental dyscalculia (DD), but recent studies suggest the relation stems from inhibitory control demands from incongruent visual cues in the nonsymbolic number comparison task. This study investigated the relation among magnitude perception during differing congruency conditions, executive function, and mathematics achievement measured longitudinally in children (n = 448) from ages 4 to 13. This relation was investigated across achievement groups and as it related to mathematics across the full range of achievement. Only performance on incongruent trials related to achievement. Findings indicate that executive function in a numerical context, beyond magnitude perception or executive function in a non-numerical context, relates to DD and mathematics across a wide range of achievement.

Mathematical thinking pervades nearly all aspects of modern life, from personal accounting to understanding important information about one's health. Accordingly, individuals with poor mathematical skills are less likely to graduate high school, go to college, have steady employment (Bynner & Parsons, 2006; Rivera-Batiz, 1992), and are at a higher physical and mental health risk (Bynner & Parsons, 2006; Duncan et al., 2007; Hibbard et al., 2007). The development of mathematical skills can be affected by a range of factors including education, home environment, and reading ability. However, a substantial body of research indicates that individual differences in the cognitive system used to perceive and manipulate numerical magnitudes, often labeled the approximate number system (ANS; Feigenson, Dehaene, & Spelke, 2004), play a foundational role in mathematics development (Chen & Li, 2014; Schneider et al., 2017; Schwenk et al., 2017). Furthermore, an estimated 3%–6% of the population is affected by the specific mathematics learning disability developmental dyscalculia (DD;

Shalev, Auerbach, Manor, & Gross-Tsur, 2000; Szűcs & Goswami, 2013). Individuals with DD display difficulties with fundamental aspects of numerical processing from very early ages and continue to struggle with math, even when given the same schooling opportunities as their peers. However, the nature of these numerical deficits and their relation to the abilities of typically developing (TD) populations remains poorly understood.

The ANS, Mathematics Achievement, and Dyscalculia

The most commonly used behavioral measure of ANS function is the nonsymbolic number comparison task. In this task, participants judge which of two groups of objects, such as dots or squares, is more numerous. Higher accuracy rates and faster response times are thought to indicate higher acuity and enhanced efficiency of the ANS (Inglis & Gilmore, 2014). There is considerable support for a relation between efficiency of the ANS and mathematics achievement, both as a marker for DD (for reviews, see Iuculano, 2016; Szkudlarek & Brannon, 2017) and across the full range of mathematics achievement (for meta-analyses, see Chen & Li, 2014; Schneider et al., 2017).

Accordingly, the dominant theory regarding a core deficit in DD proposes an impairment of the ANS, in part because individuals with DD have been shown to perform more poorly in tasks

designed to measure the ANS, such as the nonsymbolic number comparison task (Mazzocco, Feigenson, & Halberda, 2011; Mejias, Mussolin, Rousselle, Grégoire, & Noël, 2012). Furthermore, neuroimaging research suggests that individuals with DD have atypical structure and function of proposed neural substrates of the ANS, such as the intraparietal sulcus (Ashkenazi, Black, Abrams, Hoeft, & Menon, 2013; Dinkel, Willmes, Krinzinger, Konrad, & Koten, 2013; Kaufmann et al., 2009; Mussolin et al., 2010; Price, Holloway, Räsänen, Vesterinen, & Ansari, 2007; Rosenberg-Lee et al., 2015; Rotzer et al., 2008; Rykhlevskaia, Uddin, Kondos, & Menon, 2009). Given this evidence, many researchers suggest that deficits in symbolic number processing, arithmetic fluency, and higher order mathematical thinking stem from a core deficit in the ANS (Butterworth, Varma, & Laurillard, 2011; Iuculano, Tang, Hall, & Butterworth, 2008; Wilson & Dehaene, 2007).

Although there is some consensus that the ANS is atypical in individuals with DD, there is much disagreement as to the true mechanistic nature of this deficit (Szűcs & Goswami, 2013), its causal role in DD (Mazzocco & Rasanen, 2013), and whether the deficit is isolated to the ANS or may be concomitant with deficits in symbolic representation of number or issues related to executive functions (Fias, Menon, & Szucs, 2013; Rousselle & Noël, 2007; Szűcs, Devine, Soltesz, Nobes, & Gabriel, 2013). It should be further stated that the developmental relation between the ANS and the acquisition of symbolic number faculty is both important and not well understood. It is important in that mathematics is inherently symbolic, and further, most symbolic number tasks have a significantly stronger relation to math achievement than nonsymbolic tasks (De Smedt, Noël, Gilmore, & Ansari, 2013; Fazio, Bailey, Thompson, & Siegler, 2014; Geary et al., 2018; Holloway & Ansari, 2009; Schneider et al., 2017). Therefore, the importance of the ANS for math development may depend on its relation to the acquisition of symbolic number (Reynvoet & Sasanguie, 2016; vanMarle et al., 2018) or their continued relation throughout development (Leibovich & Ansari, 2016), but remains a matter of considerable debate.

Adding to this complication, individual differences in ANS acuity consistently correlate with mathematics across the full range of achievement (Halberda, Mazzocco, & Feigenson, 2008; Keller & Libertus, 2015; Schneider et al., 2017), suggesting the relation is not isolated to group differences that identify severe mathematics deficits but rather extends broadly across achievement levels. As a result, it remains unclear whether DD represents a qualitatively distinct subgroup with distinct cognitive deficits or is the lowest extreme of a continuous distribution. This distinction is important for developing appropriate intervention strategies to remediate low mathematics skills (Butterworth & Kovas, 2013; Henik, Rubinsten, & Ashkenazi, 2011). For example, if individuals with DD are identified as suffering from a specific impairment of magnitude processing that is qualitatively distinct in its mechanistic origin from their TD peers, it would suggest that remediation should target the training of this uniquely impaired mechanism.

Nonsymbolic Number Comparison as a Measure of the ANS?

One problem undermining the link between ANS function and mathematics development is the reliance on nonsymbolic number comparison as a measure of ANS acuity. Conventionally, nonsymbolic number comparison performance has been interpreted as a measure of ANS function (De Smedt et al., 2013). However, recent research suggests that the task may be measuring more than ANS acuity alone. Specifically, several studies have shown that nonsymbolic number comparison is highly influenced by the visual parameters of task stimuli (Gebuis & Reynvoet, 2011, 2012; Leibovich & Henik, 2013; Szűcs, Nobes, et al., 2013). For example, Szűcs, Devine, et al. (2013) and Szűcs, Nobes, et al. (2013) showed that congruency effects have a large impact on the ratio-based internal Weber fraction, or w, a common metric of measuring ANS acuity. Furthermore, the impact was even greater for children than in adults, leading them to suggest the visual parameter confound could also be complicated by an interaction with development. In general, visual properties such as surface area and object size covary with numerosity. If these properties are not controlled when creating stimuli, participants can rely on non-numerical cues to select the more numerous array. Thus, to ensure participants employ a strategy focused on numerosity, stimuli are designed such that, in some trials, the more numerous dot set has a greater surface area or dot size (congruent trials), and in other trials a lesser surface area or dot size (incongruent trials; e.g., Dehaene, Izard, & Piazza, 2005).

Recent studies suggest that performance on incongruent trials may drive the relation between nonsymbolic number comparison and mathematics performance (Bugden & Ansari, 2016; Clayton,

Gilmore, & Inglis, 2015; Cragg, Keeble, Richardson, Roome, & Gilmore, 2017; Fuhs & McNeil, 2013; Gilmore et al., 2013; Keller & Libertus, 2015). For example, in a study comparing nonsymbolic number comparison performance in children with DD versus TD peers, Bugden and Ansari (2016) found that children with DD only differed on incongruent trials. A follow-up analysis showed that children's visuospatial working memory predicted ANS acuity on incongruent trials, indicating that visuospatial working memory may be an important cognitive process utilized for extraction of numerosity in the presence of other visually salient information. Similarly, studies by Gilmore et al. (2013) and Fuhs and McNeil (2013) found that only performance on incongruent trials of the nonsymbolic number comparison task was related to mathematics performance across a wide range of mathematics achievement in primary school and preschoolers, respectively. To explain this specific relation, the authors of those studies suggest that incongruent, non-numerical visual cues in the comparison task require participants to inhibit their visually based response before making a quantity-based judgment, thus engaging inhibitory control mechanisms. Accordingly, both Gilmore et al. and Fuchs and McNeil posit that inhibitory control and selective attention demands of incongruent trials, rather than ANS acuity, drive the relation between nonsymbolic comparison performance and mathematics. Indeed, after controlling for inhibitory control, the relation between mathematics performance and nonsymbolic comparison was no longer statistically significant in both studies.

The ANS and Executive Function

Still, the contribution of executive function to the relation between nonsymbolic number comparison and mathematics performance remains unclear. In contrast to Gilmore et al. (2013) and Fuhs and McNeil (2013), both Keller and Libertus (2015) and Gilmore, Keeble, Richardson, and Cragg (2015) found that the relation between accuracy in the number comparison task and mathematics persisted when controlling for inhibitory control, which suggests the relation between number comparison performance and mathematics is not fully accounted for by domain-general inhibitory control. Starr, DeWind, and Brannon (2017) compared the relation between mathematics achievement and the influence of numerical acuity as distinct from the influence of non-numerical visual parameters on nonsymbolic number comparison performance

while also measuring inhibitory control in a non-numerical task (i.e., day/night in children and flanker in adults) in a 4- and 6-year-old sample and a sample of adults. Their results indicated that numerical acuity correlated with higher math scores in the 6-year-old sample, whereas non-numerical bias and inhibitory control did not, which, in agreement with the two previous studies, suggests that numerical discrimination relates to mathematics achievement. However, Starr et al.'s measure of non-numerical bias is a regression term that accounts for the influence of visual parameters on participants' behavior, which is somewhat distinct from performance on trials where visual information is incongruent with numerosity and would more directly address the notion of a number-specific executive function. Furthermore, it should be noted that all five of these studies focused on inhibitory control in a TD sample, whereas Bugden and Ansari's (2016) findings related performance on incongruent trials of the nonsymbolic comparison task to group differences between DD and TD children. In addition to the group differences versus individual differences distinction between studies, Bugden et al. investigated the role of visuospatial working memory as opposed to inhibitory control.

Although dominant models indicate that executive function can be divided into the broad categories of working memory/updating, inhibitory control, and attention shifting (Bull & Scerif, 2001; Miyake et al., 2000), most prior studies on nonsymbolic comparison and mathematics achievement have controlled for only one aspect of executive function, either working memory or inhibitory control. As a result, the more fine-grained mechanistic relations between executive function deficits and ANS deficits have been difficult to determine. To address these issues, this study focuses on two outstanding questions regarding the relation among the ANS, executive function, and mathematics achievement in typically and atypically developing individuals in order to provide more information about the specific mechanisms at play during nonsymbolic number comparison.

First, what are the mechanisms underlying the relation between performance on incongruent trials of the nonsymbolic comparison task and mathematics achievement as compared to congruent trials? Previous studies have framed the correlation between nonsymbolic comparison performance and mathematics achievement as attributable to *either* individual differences in the ANS *or* executive function. An additional possibility is that incongruent trials on the nonsymbolic number comparison task

require an *interaction* of executive function and the ANS, or in other words, a *number-specific executive function*. Rather than the relation between number comparison performance and math achievement depending on neurocognitive mechanisms associated with numerical magnitude processing or executive function independently, a deficit could originate from the biological interplay of these two mechanisms. Successfully answering an incongruent trial requires selective attention to the discrete quantity of each dot set while ignoring other salient, yet irrelevant, stimulus dimensions. Consistent with this suggestion, experimental studies have demonstrated a distinction between executive function related to numerical and non-numerical content. In a study of DD adults, individuals with DD had difficulty recruiting attention to numerical information but not non-numerical information under heightened cognitive load (Ashkenazi, Rubinsten, & Henik, 2009). In children, Bull and Scerif (2001) demonstrated that inhibitory control and working memory of numerical information accounts for significant variance in individual differences in mathematics ability beyond similar, non-numerical measures of executive function. Therefore, to appropriately account for the possibility of an interaction between executive function and the ANS, executive function must be measured in both non-numerical and numerical contexts.

Second is the relation among executive function, nonsymbolic number comparison, and mathematics achievement a specific facet of atypical development, comprising a characteristic of DD that sets the disorder qualitatively apart from typical developmental trajectories, or is the relation a characteristic of a broad range of typical mathematics skill development? Previous research appears to suggest that measurements of the ANS correlate with mathematics across the full range of mathematics achievement (Schneider et al., 2017). At the same time, studies suggest that the ANS of individuals with DD is neurobiologically atypical and functions differently than that of their TD peers (Mazzocco et al., 2011; Price et al., 2007). Distinguishing between these alternatives may provide meaningful implications for intervention strategies.

This Study

To address the questions above, this study investigates the relations among ANS function, executive function, and DD by examining performance on the nonsymbolic comparison task, separately for congruent and incongruent trials while controlling for

multiple aspects of executive function. Importantly, executive function here is measured in a non-numerical context. To build directly on previous work, we take a similar approach as Mazzocco et al. (2011). We first compare performance in the nonsymbolic comparison task across multiple mathematics achievement groups (DD, low achieving [LA], and typically achieving [TA]) defined through multiple years of consistent achievement, including the first 3 years of school entry. Second, we consider the relation between performance on the nonsymbolic comparison task and mathematics achievement more broadly through a regression analysis with a large sample that includes the full range of mathematics achievement. In the first analysis, if DD is characterized by a distinct core deficit of the ANS, performance on both congruent and incongruent trials of the task should distinguish among achievement groups. If, on the other hand, DD is characterized by deficits specific to executive function, performance on only the incongruent trials of the nonsymbolic comparison task should account for achievement group differences but not after controlling for measures of non-numerical executive function. However, if impaired number-specific executive function underlies DD, we would expect group differences between the DD group and the other achievement groups on incongruent trials, but not congruent trials, after controlling for non-numerical, domain-general executive functioning. Similarly, in the second analysis, if number-specific executive function is related to individual differences in mathematics achievement across a wide range of achievement, not only a distinction between DD and the other achievement groups, performance on incongruent trials should predict mathematics achievement beyond what can be accounted for by congruent trials and multiple components of non-numerical executive function.

Method

Participants

The current sample was drawn from a study of students who participated in an earlier longitudinal study of early mathematical skills (Pre-K to first grade; Hofer, Lipsey, Dong, & Farran, 2013). The analytic sample for the original study included 771 children. In the follow-up study, we were able to locate 628 students attending public school in the 2013–2014 year in the same district as they attended in Pre-K (16 had withdrawn from the study in first grade and were not contacted for further

participation, 29 had moved out of the state, 53 had moved out of the district, and 45 were not located despite all efforts). Of those 628, we obtained parental consent and assessed 517 children in the 2013–2014 school year, 506 children in the 2014–2015 school year, and 503 children in the 2015–2016 school year. 497 children were assessed at all three time points in middle school. English language learners ($n = 43$) were excluded because non-native language of mathematics instruction could lead to low mathematics achievement for reasons other than the cognitive factors investigated in this study.

Our final sample comprised 448 students for whom we had measures of mathematics achievement from two of the three early time points (spring of preschool, kindergarten, and first grade) and from two of the three later time points (fifth, sixth, and seventh grades), reading achievement measured at the end of kindergarten, inhibitory control and task switching measured at sixth or seventh grade, and working memory measured at fifth or sixth grade. This represents a loss of 26 students due to missing data for any of these measures from the full middle school follow-up sample ($n = 517$), or 5.0%, and only complete cases given the above criteria are analyzed. Methods for resolving differences in measurement year are described below in the description of each measure.

The final sample was 56.5% female, 9.6% White, 87.1% Black, 0.7% Hispanic, 1.1% Middle Eastern, 0.2% Asian or Pacific Islander, and 1.3% other races (no further distinction of race available). Of the 448 students who should have been in sixth grade in the 2014–2015 school year if they had not been retained or promoted early, 78 (17.4%) were still in fifth grade and 1 (0.2%) had been promoted to seventh grade. Students were located in 76 schools in the first year of the follow-up study (fifth grade), including 31 elementary schools, 27 middle schools, 11 charter schools, and 7 Innovation Cluster schools (i.e., schools that had been targeted for additional resources to boost achievement). Family income level was inferred on the basis of whether participants qualified for free or reduced lunches (i.e., family income < 1.85 times the U.S. federal income poverty guideline). In the current sample, 88.6% of participants qualified for free and reduced lunch, 10.3% did not, and 1.1% individuals were missing economic status data. Pre-K through first grade and fifth through seventh-grade waves of data collection were used to define mathematics achievement groups. Nonsymbolic comparison performance was utilized from sixth grade because concurrent measures of working memory and executive function

were available for children in that year. Mean age at the end of pre-K, the first data point, was 5.1 years ($SD = 0.3$, range = 4.5–6.4). See Table S1 for full descriptive statistics.

Achievement Groups

Individuals were placed in achievement groups if their mathematics achievement scores were consistently in the designated achievement range at two of the three early assessments (pre-K–first grade) AND two of the three later assessments (fifth–seventh grades). Given these criteria, 222 children fit into consistent achievement groups across early and later assessment periods, thus excluding 226 children, respectively, from the full sample of 448 whose achievement level varied beyond the defined threshold across time points. Descriptive statistics for the achievement group sample ($n = 222$) are broken down by achievement group in Table 1.

Our first set of analyses asked whether performance on congruent or incongruent trials of nonsymbolic number comparison distinguished children with DD from their LA and TA peers. One commonly used threshold for defining DD is performance in the lowest 10th percentile of standardized mathematics achievement tests (Dinkel et al., 2013; Mazzocco et al., 2011). Several studies comparing groups of student achieving in the lowest 10th percentile to those in the 11th–25th percentiles reveal important qualitative differences in cognitive profiles (Geary, Hoard, Byrd-craven, & Nugent, 2007; Mazzocco & Myers, 2003), notably indicating that the lowest achievement group had an impairment in nonsymbolic magnitude processing compared to all other achievement groups (Mazzocco et al., 2011). Therefore, in this study, we assigned participants to three different mathematics achievement groups, DD individuals (≤ 10th percentile), LA individuals (10th–25th percentile), and TA individuals (25th–95th percentile). With these grouping criteria, 22 children met the criteria for DD, 12 for LA, and 188 for TA. Only one individual consistently scored > 95th percentile, a commonly used criterion for school placement in gifted and talented programs, and a common threshold for designating high achieving groups in research (e.g., Hoard, Geary, Byrd-craven, & Nugent, 2008; Mazzocco et al., 2011). This individual was removed from further analysis.

There is a great diversity in definitions and cut-off thresholds for defining DD in prior literature, and accordingly, findings may not hold across different criteria for selecting DD groups. To address this heterogeneity in the literature, group

Table 1
Descriptive Statistics for Achievement Subgroups

Achievement group sample	DD (*n* = 22, 7 female)			LA (*n* = 12, 6 female)			TA (*n* = 188, 106 female)		
	M	SD	Range	M	SD	Range	M	SD	Range
Age (years), pre-K	5.1	0.5	4.5 – 6.4	5.0	0.3	4.7 – 5.5	5.1	0.3	4.5 – 5.6
Age (years), sixth grade	12.2	0.5	11.4 – 13.4	12.0	0.3	11.6 – 12.5	12.0	0.3	11.4 – 12.6
Nonsymbolic comparison (accuracy, %)	71.5	5.3	62.9 – 81.4	78.2	6.4	70.0 – 87.1	75.8	5.0	58.6 – 91.4
Nonsymbolic comparison (congruent accuracy, %)	78.7	9.1	63.6 – 90.9	76.9	10.7	54.5 – 86.4	76.3	11.1	40.9 – 95.5
Nonsymbolic comparison (incongruent accuracy, %)	53.5	13.3	27.8 – 83.3	70.8	21.3	33.3 – 94.4	65.7	14.0	33.3 – 94.4
Nonsymbolic comparison (Weber fraction, w)	0.37	0.11	0.21 – 0.65	0.26	0.10	0.13 – 0.48	0.27	0.07	0.10 – 0.56
Backward Corsi (z-score of max span)[a]	−1.21	1.22	−2.4 – 0.95	0.03	0.57	−0.75 – 0.95	0.37	0.85	−2.44 – 2.65
Hearts and flowers (z-score of accuracy, %)[a]	−1.29	0.79	−2.33 – 0.82	−0.16	0.83	−1.90 – 1.83	0.40	0.83	−1.90 – 1.83
Letter-word identification (WCJ–III, standard score)	91.4	9.90	75 – 113	97.4	11.9	73 – 113	115.1	11.9	85 – 144

Note. WCJ–III = Woodcock Johnson–III; DD = developmental dyscalculia; LA = low achieving; TA = typically achieving.
[a]z-scores presented based on full sample of 448 individuals.

comparison analyses in this study were replicated with another commonly used threshold for determining DD (achievement < 1.5 *SD* below the population mean) and included in Appendix A. Using this alternative threshold did not alter the results, suggesting the results are not a product of the chosen threshold.

Many previous studies have attempted to isolate the neurocognitive mechanisms of DD by studying a group of individuals with DD compared to a control group matched on IQ and other cognitive abilities (Landerl, Bevan, & Butterworth, 2004; Mussolin et al., 2010; Rotzer et al., 2008). This study does not take this approach for two reasons. First, research suggests that defining learning disability groups through discrepancy criteria excludes many individuals with dyscalculia who suffer from comorbid learning disabilities or other developmental issues. Most estimates suggest that 20%–40% of individuals with DD also have dyslexia (Shalev, 2004; Willcutt et al., 2013; Wilson et al., 2015), and around 25% also have attention deficits (Landerl, Göbel, & Moll, 2013; Shalev, 2004; Shalev, Auerbach, & Gross-Tsur, 1995). This suggests that DD is inherently heterogeneous and would better be characterized by a framework whereby individuals are designated as DD through proof of consistent, low mathematics achievement over time with the presence of adequate educational opportunity (Fuchs, Morgan,

Young, & Rise, 2003). Therefore, rather than exclude nondiscrepant individuals, this study follows previous literature (Mazzocco et al., 2011) and investigates differences in the ANS while controlling for reading achievement and domain-general executive function. Second, this study examines the intersection of attention mechanisms and magnitude processing mechanisms. Any attempt to define groups as a function of broader measures of achievement would impede investigation of individual differences in executive function, which is known to correlate with academic achievement.

Procedure

All students assented and students' families consented to participate, and the study was approved by the university's institutional review board. Assessments were conducted by trained members of the research staff. The nonsymbolic number comparison task and executive function tasks were administered during the spring semester of the students' sixth-grade year via tablet computer. Testing for mathematics achievement was completed in a quiet location at the students' school with one-to-one assistance from trained staff during the student's pre-K, kindergarten, first-grade, fifth-grade, sixth-grade, and seventh-grade years. Reading achievement was assessed at the end of kindergarten.

Cognitive Tasks

Nonsymbolic Number Comparison

Participants were presented with two sets of dots simultaneously and asked to indicate via button press which set was more numerous (i.e., which set contained more dots). The set on the left side of the screen contained yellow dots and the set on the right side contained blue dots, which corresponded to color-coded left and right buttons. Response sides were fully counterbalanced. Trials consisted of 1,200 ms stimulus presentation followed by 1,800 ms of fixation (see Figure 1). Seven ratios were presented, 0.33 (5 dots vs. 15 dots), 0.5 (5 vs. 10), 0.67 (6 vs. 9), 0.8 (8 vs. 10), 0.86 (12 vs. 14), 0.88 (7 vs. 8), 0.9 (9 vs. 10). The number of dots in each stimulus ranged from 5 to 15. Each ratio was presented 10 times for a total of 70 trials, which were preceded by six practice trials of the easiest two ratios.

If individuals did not correctly respond to at least four of the six practice trials, practice trials were repeated up to two times. If participants did not answer four of six correctly on any practice run, they did not proceed to the experimental trials. Ratios, stimulus presentation times, and order of presentation were modeled after Odic, Hock, and Halberda (2014). To control for the possibility that participants might utilize a strategy based on visual cues rather than number of dots, the following visual properties of dot sets were varied using a modified version of the MATLAB code recommended by Gebuis and Reynvoet (2011): convex hull (area extended by a stimulus), total surface area (aggregate value of dot surfaces), average dot diameter, total circumference, and density (convex hull divided by total surface area). In
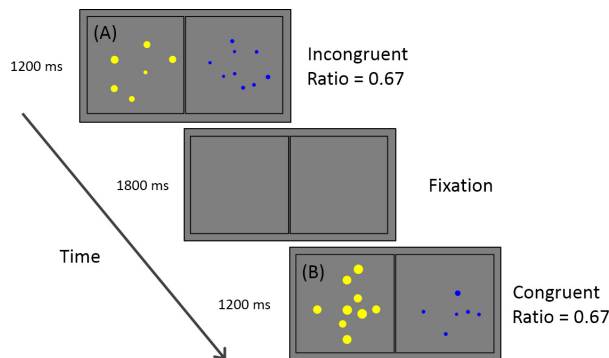
approximately one quarter of the trials (22 of 70), all four visual properties were congruent with greater numerosity (i.e., the greater number of dots had a greater convex hull, surface area, etc.). In another quarter of the trials (18 of 70), all four visual properties were incongruent with greater numerosity. In the remaining trials, visual properties were mixed congruent and incongruent.

Analyses of task effects include all trials. Analyses directly addressing the research questions include trials that were either fully congruent (22 trials) or incongruent (18 trials) on all five visual parameters. Mixed congruency trials were excluded. Congruent versus incongruent trials per ratio are not perfectly balanced in trial numbers, but the average ratio for each is nearly identical (average ratio congruent = 0.733, average ratio for incongruent = 0.744; for further details, see Table S2). Performance was calculated as mean number of items correct and as a Weber fraction (Halberda et al., 2008) to facilitate comparison with previously published research. However, the model implementing Levenberg–Marquardt least squares fit used to calculate Weber fractions did not provide a sufficient fit with the fewer number of trials available within congruency conditions (as indicated by whether the model predicted a significant amount of variance, $p < .05$). Furthermore, a growing body of literature suggests that mean accuracy is strongly correlated with and possibly more reliable than ratio-dependent metrics such as the Weber fraction (Gilmore, Attridge, & Inglis, 2011; Inglis & Gilmore, 2014), which is true even in the case of congruency comparisons (Szűcs, Devine, et al., 2013; Szűcs, Nobes, et al., 2013). Therefore, in this study, mean accuracy percentages were used instead of Weber fractions to index performance on each of our number comparison tasks.

Figure 1. Nonsymbolic numerical magnitude comparison stimuli and paradigm timing. (A) Incongruent trial example of ratio 0.67 (smaller number dot set/larger number dot set, 6/9 = 0.67). (B) Congruent trial example, also of ratio 0.67.

Working Memory

The backward Corsi block-tapping test (Corsi, 1972) provided a measure of visuospatial working memory. In this computerized task, children first viewed squares that lit up in a sequence on the screen, and then the students were asked to tap the squares in the reverse order in which they lit up. The task consisted of 16 total possible trials, including two practice trials. The student was given two attempts to correctly repeat the reverse sequence per sequence length, increasing in span from 2 to 8 across the task. If the student correctly answered at least 1 of the 2 attempts correctly, the student then proceeded on to the longer (more difficult)

sequence. The score of interest was the highest span with a correctly repeated sequence. For some children without sixth-grade Corsi spans, 22 children of $n = 448$, fifth-grade spans are utilized. For details, see Appendix B.

Inhibitory Control and Task Switching

The hearts and flowers task (Wright & Diamond, 2014) was used as measure of students' task switching and inhibitory control. In this task, the child was first presented with a heart on either side of the screen and instructed to press the button that corresponds to the side of the screen with the heart. This first block comprised 12 trials. In the second block of trials (also 12 trials), the child was presented with flowers and asked to press the button that is opposite the side of the flower. In the third set of trials, the child was randomly presented with either a heart or a flower and asked to follow the rule that corresponds to hearts and flowers, respectively. The third block comprised 48 trials. To index executive function, we used mean accuracy from the third, mixed-condition block of trials, and as such, this single measure captures both task switching and inhibitory control (Diamond, 2014). One child was not assessed at sixth grade for Hearts and Flowers, but a score from seventh grade was available. The same z-score method described above was utilized to create a score for this child and z-scores were utilized for all subsequent analyses.

Academic Achievement

Reading Achievement: Woodcock Johnson–III—Letter-Word Identification

The Woodcock Johnson–III (WCJ–III; Woodcock, McGrew, & Mather, 2001) is a standard assessment of a range of skills, designed to be used with people ages 2–90+. The letter-word identification (LWID) subtest assesses children's letter and sight word identification ability with the correct pronunciation. Items include identifying and pronouncing letters and words presented to the child (e.g., "A" or "dog"). Age-normed standard scores were calculated as an early measure of reading achievement measured at the end of kindergarten and then converted to percentile ranks.

Mathematics Achievement

WCJ–III Quantitative Concepts and Applied Problems subtests were used as measures of mathematics achievement during the early school years (Pre-K–first grade) and KeyMath-3 (KM-3) subscales of Numeration, Algebra, and Geometry were used for the middle school time points (fifth–seventh grade). Standard scores from each measure were converted to percentile rank scores based on the nationally normed mean and standard deviations of the sample utilized for each respective standardized assessment. Percentile rank scores were utilized for (a) achievement group creations based on percentile rank threshold in the first analysis and (b) the principal outcome variable of interest in our multilevel regression analysis.

WCJ–III—Quantitative Concepts and Applied Problems. Quantitative Concepts and Applied Problems subtests were administered at the end of each school year during Pre-K, kindergarten, and first grade. Individually administered, Quantitative Concepts has two parts and assesses students' knowledge of mathematical concepts, symbols, and vocabulary, including numbers, shapes, and sequences; it measures aspects of quantitative mathematics knowledge and recognition of patterns in a series of numbers. The Applied Problems subtest is an untimed verbal and picture-based measure of a student's ability to analyze and solve mathematics problems, beginning with the application of basic number concepts. At each early time point, age-normed standard scores were calculated for each subtest and averaged together to create a composite measure of mathematics competence representing a broad range of mathematics skills. These scores were subsequently converted to percentile ranks.

KeyMath-3. The KM-3 Diagnostic Assessment (Connolly, 2007) is a comprehensive, norm-referenced measure of essential mathematical concepts and skills. It was administered at the end of each school year during fifth, sixth, and seventh grades. We used three subscales out of the five subscales in the Basic Concepts area. (a) Numeration: The Numeration subtest measures an individual's understanding of whole and rational numbers. It covers topics such as identifying, representing, comparing, and rounding one-, two-, and three-digit numbers as well as fractions, decimal values, and percentages. It also covers advanced numeration concepts such as exponents, scientific notation, and square roots. (b) Algebra: The Algebra subtest measures an individual's understanding of prealgebraic and algebraic concepts. It covers topics such as sorting, classifying, and ordering by a variety of attributes; recognizing and describing patterns and functions; working with number sentences, operational properties, variables, expressions, equations,

proportions, and functions; and representing mathematical relations. (c) Geometry: The Geometry subtest measures an individual's ability to analyze, describe, compare, and classify two and three-dimensional shapes. It also covers topics such as spatial relations and reasoning, coordinates, symmetry, and geometric modeling. Scale scores in the KM-3 are age normed to reflect population means of 10 (SD = 3) for each subtest. We averaged scale scores from the three subscales into a composite measure (KM composite) as in previous analyses involving the current sample (Price & Wilkey, 2017; Rittle-Johnson, Fyfe, Hofer, & Farran, 2017). This score was then converted to a percentile rank to compose mathematics achievement groups across measures of mathematics achievement in the early grades (Pre-K–first grade) and late measures of mathematics achievement (fifth grade to seventh grade).

The relation between KM-3 scores and predictor variables was nonlinear based on visual inspection of scatter plots, so when conducting analyses that assumed a linear relation (e.g., bivariate correlation, partial correlation, or regression), models were fit using a transformed outcome (i.e., cubed root) of KM-3 percentile rank. A detailed exploration of the untransformed achievement scores' relation to predictor variables is detailed in Appendix C.

Analysis

To investigate group differences among DD, LA, and TA groups on nonsymbolic comparison on both congruent and incongruent trials, we conducted a two-way (3 × 2), mixed effects analysis of variance (ANOVA) with achievement group as a between-subject factor, congruency condition of nonsymbolic comparison as a within-subjects factor, and accuracy rate on the nonsymbolic comparison task at sixth grade as the dependent variable. Levene's tests were run for each ANOVA to analyze violations of homogeneity of variance that often results from unequal sample sizes. When violated, Welch's adjusted F was used for the ANOVA and noted in the results. One-way post hoc t-tests were conducted to examine simple main effects and pairwise differences where appropriate. Bonferroni-corrected p-values are reported to correct for multiple comparisons for all subsequent analyses and to ensure tests were robust against violations of homogeneity of variances between groups. Effect sizes are reported as Hedge's g, which accounts for unequal group ns by weighting the pooled standard deviation according to group size, $\frac{M1-M2}{SD_{\text{pooled,weighted}}}$.

Because clustering of students within schools did not account for a significant proportion of variation in sixth-grade nonsymbolic number comparison accuracy ($\hat{\rho}$ = .009, p = .74), a multilevel modeling approach to account for the clustering of students within schools was not needed.

The second set of analyses used random effects multilevel models to predict sixth-grade mathematics achievement from concurrent experimental measures. This analysis examined whether individual differences in nonsymbolic number comparison performance related to standardized mathematics achievement across a wide range of achievement. Specifically, we examined whether sixth graders' accuracy on nonsymbolic number comparison for incongruent and congruent trials predicted concurrent mathematics achievement for the full sample of students (n = 448), and whether the relation changed when controlling for early reading achievement and domain-general executive functioning.

Results

Task Effects

Nonsymbolic comparison task performance profiles were consistent with previous findings (e.g., Lyons, Nuerk, & Ansari, 2015), showing a significant effect of ratio on mean accuracy for all trials [F(6, 447) = 1,255.22, p < .001, partial η^2 = .737], and within congruency conditions [F(6, 447) = 339.01, p < .001, partial η^2 = .431 for congruent trials; F(6, 447) = 401.17, p < .001, partial η^2 = .473 for incongruent trials]. Furthermore, both mean accuracy and Weber fraction were correlated with mathematics achievement at sixth grade (mean accuracy Pearson r(446) = .191, p < .001, 95% CI [.100, .278]; Weber fraction Pearson r(446) = −.244, p < .001), 95% CI [−.329, −.155], which is in line with a recent meta-analysis reporting an average correlation of r = .241 (k = 195) between nonsymbolic comparison and a broad range of mathematics achievement measures across multiple age groups (Schneider et al., 2017). Mean accuracy and Weber fractions were highly correlated (Pearson r(446) = −.919, p < .001), 95% CI [−.932, −.903].

Achievement Group Comparison Results

Results of the two-way ANOVA indicated a main effect of achievement group [F(2, 219) = 6.694, p = .002, partial η^2 = .058], a main effect of congruency [F(1, 219) = 27.570, p < .001, partial η^2 = .112] whereby individuals were more accurate on

congruent trials, and an interaction [F(2, 219) = 4.816, p = .009, partial η^2 = .042]. To characterize the main effect of achievement group, we conducted between-subjects t-tests comparing accuracy on the combined congruent and incongruent trials. Accuracy rate was 6.7 points [95% CI: 2.6, 10.9] lower for the DD group than the LA group [t(32) = −3.293, Bonferroni adjusted (α/3) p = .003, unadjusted p < .001, Hedge's g = 1.182] and 4.3 points [95% CI: 2.0, 6.5] lower for the DD group than the TA group [t(208) = −3.761, Bonferroni adjusted (α/3) p = .002, unadjusted p < .001, Hedge's g = 0.847]. There was no significant difference between the LA and TA groups [t(198) = 1.619, Bonferroni adjusted (α/3) p = .161, unadjusted p = .053, Hedge's g = 0.482].

The Effect of Congruency

Pairwise comparisons were conducted to characterize the simple effect of congruency within achievement groups. There was an effect of congruency in the DD and TA groups whereby, on average, the DD group accuracy rate was 25.2 points [95% CI: 16.6, 33.8] lower for incongruent compared to congruent trials [t(21) = 6.076, Bonferroni adjusted (α/3) p < .001, unadjusted p < .001, Hedge's g = 2.203] and the accuracy rate for the TA group was 10.7 points [95% CI: 7.6, 13.8] lower for incongruent compared to congruent trials [t(21) = 6.795, Bonferroni adjusted (α/3) p < .001, unadjusted p < .001, Hedge's g = 0.844]. However, there was no effect of congruency in the LA group [t(11) = 0.716, Bonferroni adjusted (α/3) p = .732, unadjusted p = .244, Hedge's g = 0.359] (see Figure 2 and Table 1 for means).

The Effect of Achievement Group

To characterize the simple effects of achievement group, one-way analyses of variance (ANOVAs) were conducted within congruency conditions, followed by pairwise comparisons of achievement groups. Results from the ANOVA on accuracy for congruent trials showed no effect of achievement group [F(2, 219) = 0.476, p = .622, η^2 = .004] (Figure 2). Levene's test of equality of variances showed no significant differences in variance across groups for mean accuracy of congruent trials (Levene's statistic = 0.383, p = .682).

In contrast, results from the ANOVA on incongruent trials showed a significant effect of achievement group on accuracy Welch's [F(2, 21.45) = 8.345, p = .002, η^2 = .070]. Levene's test
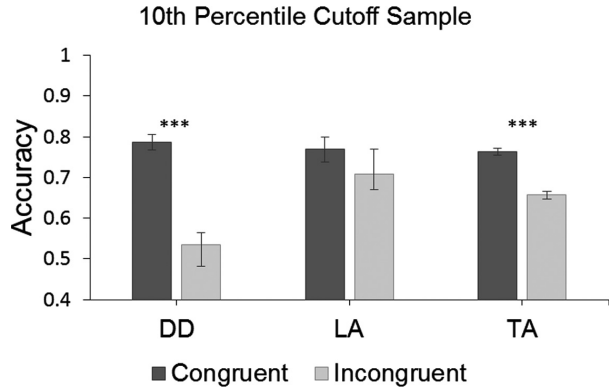

Figure 2. Nonsymbolic number comparison accuracy rates by achievement group. DD = developmental dyscalculia; LA = low achieving; TA = typically achieving. Error bars represent standard errors. p-Values are indicated for differences in accuracy between congruent and incongruent trials (***p < .001).

indicated significant differences in variance across groups for mean accuracy of incongruent trials (Levene's statistic = 4.317, p = .014); however, variance only differed between groups by a factor of 2.56 at most, so Welch's adjusted F was used for the ANOVA. After adjusting for multiple comparisons, post hoc tests of incongruent trials indicated that accuracy rate for the DD group was 17.3 points [95% CI: 5.2, 29.4] lower than the LA group [t(32) = −2.916, Bonferroni adjusted (α/3) p = .002, unadjusted p = .005, Hedge's g = 1.046] and DD accuracy rate was 12.1 points [95% CI: 5.9, 18.3] lower than the TA group [t(208) = −3.862, Bonferroni adjusted (α/3) p < .001, unadjusted p < .001, Hedge's g = 0.870]. There was no difference between LA and TA groups [t(198) = 1.197, Bonferroni adjusted (α/3) p = .350, unadjusted p = .117, Hedge's g = 0.356, mean difference = 5.2 points, 95% CI: −3.3, 13.7].

To further investigate achievement group differences after controlling for domain-general factors, analyses were repeated as a one-way analysis of covariance (ANCOVA) with the covariates of max span achieved on the backward Corsi, mean accuracy during mixed trials of the hearts and flowers task, age at time of testing, and percentile rank on the WCJ–III LWID at the end of kindergarten. After controlling for these factors, there was still a significant effect of achievement group for accuracy on incongruent trials [F(2, 215) = 4.658, p = .010, partial η^2 = .042]. After adjusting for multiple comparisons, covariate adjusted means were 16.6 points [95% CI: 3.3, 29.9] lower for the DD than the LA group [Bonferroni adjusted (α/3) p = .015, unadjusted p = .005, Hedge's g = 0.823] and 10.0 points

[95% CI: 1.0, 21.0] lower for the DD group than the TA group [Bonferroni adjusted $(\alpha/3)$ $p = .045$, unadjusted $p = .002$, Hedge's $g = 0.823$]. There was no significant difference between the LA and TA groups [Bonferroni adjusted $(\alpha/3)$ $p = .231$, unadjusted $p = .077$, Hedge's $g = 0.585$]. These results replicate the pattern observed in the ANOVA.

In sum, all ANOVAs and ANCOVAs conducted show the same pattern of results whereby: (a) no group differences are observed for congruent trials of the comparison task, (b) the DD group performs significantly below LA and TA groups on incongruent trials even when controlling for other cognitive factors and early reading achievement, and (c) no group differences are present between LA and TA groups on incongruent trials.

Full Range of Achievement Results

For descriptive statistics of the full sample, see Table 2. For bivariate correlations among measures, see Table S3. Of note is a moderate, negative bivariate correlation between accuracy rates for congruent and incongruent trials, $r(446) = -.447$, $p < .001$, 95% CI [$-.518, -.369$]; see Figure S1 for scatter plot. To investigate potential differences among subtests of the KM-3 and their correlations with performance in the nonsymbolic number comparison task, Pearson-r values were converted to z values and then compared with a two-tailed z-test. Results indicated there were no significant differences among any correlations according to KM-3 subtests (all ps $> .435$, see Table S4 for details) and all further analyses were conducted on KM-3 composite scores.

Multilevel Regression Model Predicting Mathematics Achievement

Multilevel modeling accounts for the clustering of students within schools, as approximately 23% of the variation in sixth-grade mathematics achievement was due to school membership ($\hat{\rho} = .225$, $p < .0001$). Equation 1 illustrates the modeling approach, in which $MATH_{ij}$ represents sixth-grade mathematics achievement for each student i in school j. The predictors $INCON_{ij}$ and CON_{ij} represent student-level accuracy on nonsymbolic number comparison for incongruent and congruent trials, respectively; HAF_{ij} represents student-level standardized scores on the hearts and flowers task; $CORSI_{ij}$ represents student-level standardized backward Corsi max span scores; $READ_{ij}$ represents student-level age-normed standard scores on the LWID test; and X_{ij} represents a vector of potential

Table 2

Descriptive Statistics for Experimental and Standardized Measures for Full Sample

	Entire sample ($n = 448$, 250 female)		
	M	SD	Range
Age (years), sixth grade	12.0	0.32	11.4–13.4
Nonsymbolic comparison (accuracy, %)	74.8	5.48	48.6–91.4
Nonsymbolic comparison (congruent accuracy, %)	76.6	11.2	36.4–100
Nonsymbolic comparison (incongruent accuracy, %)	63.1	14.5	22.2–94.4
Nonsymbolic comparison (Weber fraction, w)	0.29	0.10	0.10–1.42
Backward Corsi (max span)[a]	4.81	1.22	2–8
Hearts and flowers (accuracy, %)[a]	73.4	14.5	35–100
Letter-word identification—WCJ–III (K, percentile rank)	109.7	12.7	73–144
Math achievement—KM-3 (sixth grade, percentile rank)	27.0	23.1	0.5–92.5

Note. WCJ–III = Woodcock Johnson–III; KM-3 = KeyMath-3.
[a]Raw scores reported here for year available. See Sections *Working Memory, Inhibitory Control and Task Switching,* and *Appendix C* for a detailed description of scores used for analyses.

student-level covariates, such as gender or age at testing. Due to nonlinearity in the relation between mathematics scores and the predictors, models were fit using a transformed outcome (i.e., cubed root).

$$\sqrt[3]{MATH_{ij}} = \beta_0 + \beta_1 INCON_{ij} + \beta_2 CON_{ij}$$
$$+ \beta_3 HAF_{ij} + \beta_4 CORSI_{ij} + \beta_5 READ_{ij}$$
$$+ \beta_6 X_{ij} + (e_{ij} + u_j).$$

$$(1)$$

The bivariate correlations of the transformed achievement variable are presented in Figure 3 with a plot of nonsymbolic number comparison performance by congruency on achievement.

Table 3 presents parameter estimates, standard errors, significance levels, random effects, and goodness-of-fit statistics for a taxonomy of fitted models describing the relation between mathematics achievement and nonsymbolic number comparison, domain-general executive functioning, early reading achievement, and age at testing in sixth grade. The first model (i.e., M1) displays the grand mean of sixth-grade mathematics achievement, across all students and schools, and the intraclass correlation ($\hat{\rho} = .225$, $p < .0001$) that motivates the
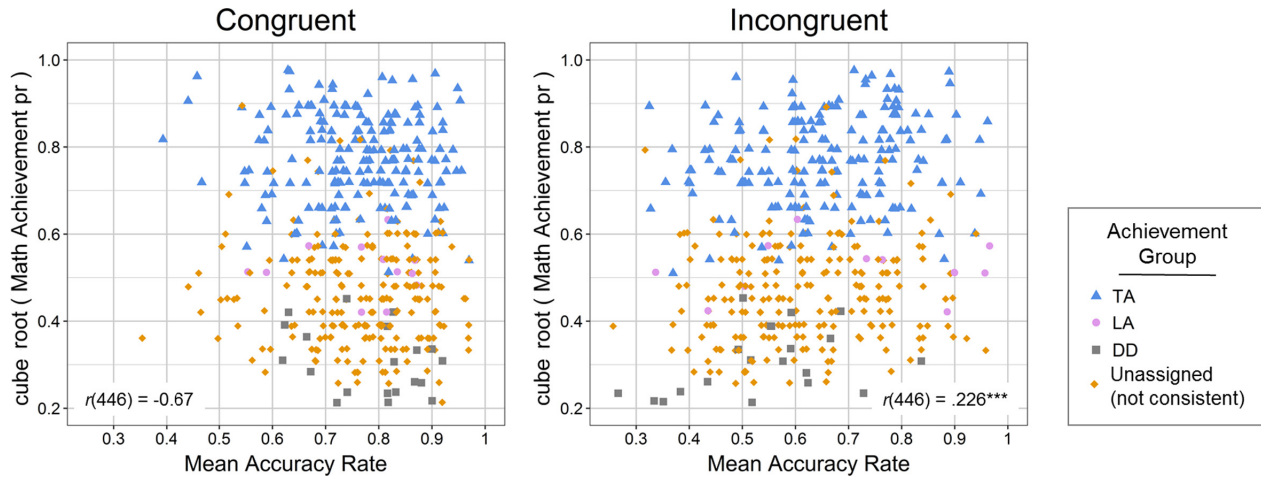
Figure 3. Nonsymbolic number comparison accuracy rates split by (left) congruent and (right) incongruent trials including all individuals from the full sample plotted against $\sqrt[3]{\text{MATH}_{ij}}$, the outcome variable of Equation 1 below, cube root of the composite math achievement percentile rank. DD = developmental dyscalculia; LA = low achieving; TA = typically achieving; pr = percentile rank. Bivariate correlations of the full sample are presented in the bottom corner of each panel (***p < .001). Orange diamonds represent individuals who did not fit our selection criteria for stable achievement grouping based on pre-K to seventh-grade achievement.

multilevel modeling approach. Model M2 shows the relations between accuracy on congruent and incongruent conditions of the nonsymbolic number comparison task and transformed sixth-grade mathematics achievement. There is a statistically significant relation between accuracy on incongruent nonsymbolic number comparison and transformed sixth-grade mathematics achievement (z = 4.88, p < .0001), but accuracy on congruent trials is not a statistically significant predictor of mathematics achievement (z = 1.16, p = .25). Accordingly, accuracy on congruent trials was excluded from subsequent models.

Subsequent models (M3–M5) show that the relation between accuracy on incongruent trials of the nonsymbolic number comparison task and transformed sixth-grade mathematics achievement persists after controlling for additional predictors of mathematics achievement. Model M3 shows the relation between accuracy on incongruent nonsymbolic number comparison trials and transformed mathematics achievement, controlling for domain-general executive functioning. Hearts and Flowers and backward Corsi performance have a statistically significant relation with mathematics achievement (z = 7.71, p < .0001 and z = 7.12, p < .0001, respectively), controlling for nonsymbolic number comparison. Parameter estimates and statistical significance of relations remain stable when controlling for reading performance in kindergarten (see Table 3, M4) and age of mathematics testing in sixth grade (see Table 3, M5), though the

magnitudes decrease slightly. Additional models were fit testing demographic variables (e.g., gender) and interaction terms among the nonsymbolic comparison and executive function predictors; however, none were statistically significant (p's ranged from .06 to .98). Furthermore, we conducted a sensitivity analysis to examine whether students with DD may be driving the relationship between performance on incongruent trials and mathematics achievement. To do so, we refit model M5 without the DD subgroup (n = 22). Results were unchanged. Taken together, the analysis suggests that student performance on incongruent trials of nonsymbolic number comparison is predictive of concurrent mathematics achievement, above and beyond non-numerical, domain-general executive functioning, early reading achievement, and age at testing in sixth grade. For detailed explanation of the model fit, see Appendix C.

Discussion

This study investigated the relation among ANS function, executive function, and mathematics achievement by examining performance on the nonsymbolic number comparison task, separately for congruent and incongruent trials, while controlling for multiple components of executive function measured in non-numerical contexts. We investigated this relation first as it relates to group differences among DD, LA, and TA students and then as a

Table 3

Taxonomy of Fitted Multilevel Models Describing the Relation Between the Cubed Root of Sixth-Grade Mathematics Achievement and Accuracy on Nonsymbolic Number Comparison, Separately for Incongruent and Congruent Trials, Controlling for Working Memory, Inhibitory Control and Task Switching, Reading Achievement, and Age of Testing in Sixth Grade ($n_{schools}$ = 75; $n_{students}$ = 448)

	Sixth-grade mathematics achievement (cubed root)				
	M1	M2	M3	M4	M5
Intercept	.562***	.286**	.480***	.011	−1.084**
	(.015) [.532 to .593]	(.091) [.107 to .465]	(.036) [.410 to .551]	(.072) [−.131 to .152]	(.337) [−1.744 to −.424]
Nonsymbolic comparison, incongruent trials, acc.		.321***	.144**	.141**	.126*
		(.066) [.192 to .449]	(.053) [.039 to .248]	(.051) [.042 to .241]	(.050) [.027 to .224]
Nonsymbolic comparison, congruent trials, acc.		.097			
		(.083) [−.066 to .261]			
Backward Corsi, max span			.054***	.051***	.050***
			(.008) [.039 to .069]	(.007) [.037 to .065]	(.007) [.036 to .064]
Hearts and flowers, mixed trials, acc.			.060***	.053***	.051***
			(.008) [.045 to .075]	(.007) [.038 to .067]	(.007) [.036 to .065]
Reading achievement, LWID, end of Kindergarten				.004***	.005***
				(.001) [.003 to .006]	(.001) [.004 to .007]
Age of KeyMath-3 testing, sixth grade					.007***
					(.002) [.003 to .011]
$\hat{\sigma}_u$	.094***	.091***	.073***	.057***	.051***
	(.014)	(.014)	(.011)	(.010)	(.010)
$\hat{\sigma}_e$	.174***	.170***	.150***	.144***	.143***
	(.006)	(.006)	(.005)	(.005)	(.005)
$\hat{\rho}$	.225***	.223***	.190***	.134***	.112**
	(.057)	(.057)	(.050)	(.043)	(.040)
Log-likelihood	114.559	126.743	185.816	211.721	217.176

Note. Standard errors are in parentheses and 95% confidence intervals are in brackets. Acc. = accuracy; LWID = letter-word identification; $\hat{\sigma}_u$ = school-level residual standard deviation; $\hat{\sigma}_e$ = student-level residual standard deviation; $\hat{\rho}$ = intraclass correlation.
*p < .05. **p < .01. ***p < .001.

factor related to mathematics across a full range of achievement. Results indicated that a dynamic interplay of the ANS and executive function mechanisms, beyond either mechanism alone, represents a deficit specific to DD and is also related to mathematics across a full range of mathematics achievement. Together, the current findings suggest that a focus on ANS alone is insufficient to explain the relation between basic number processing and mathematics outcomes. Therefore, we suggest that our results point to a need to reframe existing models of the relation between number processing and mathematics competence to include the relation between executive function mechanisms and magnitude processing, and to move beyond single mechanism explanations more generally.

Achievement Group Comparison

In the first analysis, we compared accuracy rates in the nonsymbolic comparison task across three mathematics achievement levels (i.e., DD, LA, and TA) defined through 6 years of consistent achievement, including the first 3 years of school entry (pre-K–first grade) and 3 later years of entry to middle school (fifth–seventh grade). Our results showed that accuracy on incongruent trials, and not congruent trials, was significantly lower for DD (defined at two different thresholds) compared to LA and TA groups, even after controlling for early reading achievement, visuospatial working, inhibitory control, and task shifting. LA and TA groups, on the other hand, did not differ from one another, thus supporting the hypothesis that an impairment in the interaction between executive function and the ANS is characteristic of individuals with DD.

Explanations of the link between ANS and mathematics achievement that involve a dynamic interaction between the ANS and executive function have considerable support from a large body of research linking low mathematics performance with various executive function impairments. These include associations between low mathematics achievement and inhibitory control (Blair & Razza, 2007; Espy et al., 2004; Szűcs, Devine, et al., 2013; Szűcs, Nobes, et al., 2013), spatial processing (Rourke & Conway, 1997), verbal and visuospatial working memory (Bull & Lee, 2014; Bull & Scerif, 2001; Geary, 2004; Lee & Bull, 2016; Szűcs, Devine, et al., 2013; Szűcs, Nobes, et al., 2013), set shifting (Willcutt et al., 2013), sustained visual attention (Anobile, Stievano, & Burr, 2013), and inattentive behaviors (Fias et al., 2013; Shalev et al., 1995). Furthermore, DD has a high rate of comorbidity with

attention-deficit/hyperactivity disorder (Czamara et al., 2013). Although the link is often made between general measures of executive function and mathematics achievement, there is evidence that the relation is specific to measures of executive function involving numerically relevant information. For example, Siegel and Ryan (1989) found that individuals with DD have impairments of working memory related to processing numerical information and not language. Experimental studies have also demonstrated a distinction between executive function to numerical and non-numerical content. Ashkenazi et al. (2009) found that individuals with DD had more difficulty recruiting attention to numerical information but not non-numerical information under heightened cognitive load compared to TD peers. This array of findings has led some to suggest that DD may involve a domain-specific executive function problem (e.g., Bull & Scerif, 2001). In other words, individuals with DD may not have a generally impaired ANS system, but rather have difficulty working with numerical magnitudes under additional executive function demands. Results from this study showing mathematics achievement group differences in nonsymbolic comparison performance only during incongruent trials, after controlling for non-numerical executive function, lend further support to this hypothesis. Whether this deficit is driven by a failure to upregulate numerical information above competing information as attention shifting would require, or perhaps a failure to disengage attention from non-numerical information by inhibiting interference from irrelevant stimulus dimensions remains an open empirical question. As the DD group's average performance during incongruent trials is around chance, little can be inferred with about strategy during these trials.

This study's results contrast with some previous studies using an alternative method for controlling visual parameters of dot stimuli, which have not found an effect of congruency on response behaviors (Odic, Libertus, Feigenson, & Halberda, 2013; Odic et al., 2014). However, in those studies, the effect of congruency may be confounded by the fact that degree of visual congruency (and incongruency) is linearly related to trial ratio. This means that in difficult ratio trials, which capture the most variance related to individual differences in ANS acuity, each dot set is very similar in terms of surface area, thus decreasing the likelihood of finding a congruency effect. Although this method may be appropriate for measurement of general ANS acuity, the effects of congruency are difficult to

separate from the effects of numerical ratio, because the two are linked so tightly. This study uses a method of controlling congruency that is more balanced across ratios and controls for a greater number of stimulus properties beyond dot size and surface area (for a detailed discussion, see Clayton et al., 2015). Therefore, the effects of congruency and ANS function are more clearly disentangled in this study.

One unexpected result from the first, group-wise analysis is that DD and TA groups showed congruency effects, as expected, but LA children did not. Despite this lack of a congruency effect in the current findings for this achievement group, we caution against any strong interpretation of this result. There is a trend in the expected direction for each of the LA children groupings (10th percentile and 6.7th percentiles cutoffs), in which children are more accurate on congruent trials than incongruent trials. Despite the lack of a significant effect, the effect sizes are relatively large (Hedge's g = 0.359 and Hedge's g = 0.71), and mean differences are 6 accuracy points and 10 accuracy points for each sample, respectively. It is likely that the absence of a statistically significant congruency effect for LA children is due to high variance in accuracy on incongruent trials and a lack of power for this comparison.

Full Range of Achievement

In the second analysis, we examined whether sixth graders' accuracy on nonsymbolic number comparison for incongruent and congruent trials predicted concurrent mathematics achievement for the full sample of students and whether the relation changed when controlling for early reading achievement and non-numerical, domain-general executive functioning. The sample for this analysis included a wide range of mathematics achievement levels that included all participants from the first analysis and participants in the broader study that did not consistently achieve in the same level year to year. Similar to the logic of the first analysis, if number-specific executive function is related to individual differences in mathematics achievement across a wide range of achievement, performance on incongruent trials should predict mathematics achievement beyond what can be accounted for by congruent trials and early reading achievement, visuospatial working memory, inhibitory control, and task shifting. Indeed, results showed that accuracy on incongruent trials predicted concurrent mathematics achievement even after controlling for

early reading achievement, visuospatial working memory, inhibitory control, and task shifting, thus supporting the hypothesis that number-specific executive function relates to individual differences in mathematics achievement across a wide range of achievement levels. Furthermore, the relation remained unchanged when we excluded individuals with DD from the regression. These findings build on previous research that has shown other number-specific measures of executive function relate to mathematics achievement in TD and high achieving groups. For example, Dark and Benbow (Dark & Benbow, 1994) found that working memory tasks with numerical stimuli were more closely related to mathematical precocity than non-numerical stimuli across a range of tasks in adults. Similarly, studies of children have demonstrated that inhibitory control and working memory of numerical information accounts for significant variance in individual differences in mathematics ability and early numeracy beyond similar non-numerical measures of executive function (Bull & Scerif, 2001; Merkley, Thompson, & Scerif, 2016).

Interestingly, bivariate correlations indicated that children with high accuracy on incongruent trials tended to have low accuracy on congruent trials (and vice versa), even though congruent trials were not related to mathematics achievement. This may be important for two reasons. First, if only incongruent trials are related to mathematics achievement, researchers may be tempted to design measures consisting exclusively of incongruent trials. However, this inverse relation may indicate that incongruent trials are inherently related to congruent trials such that removing congruent trials would change the nature of the task demands for incongruent trials. Second, speculation about inhibitory control has dominated the conversation about the cognitive mechanisms underlying the difference between incongruent trials and congruent trials of the nonsymbolic comparison task (Cragg et al., 2017; Gilmore et al., 2015). Although inhibitory control may be a factor, the inverse correlation between congruency conditions may indicate that some individuals are unable to switch between strategies that capitalize on visual cues during congruent trials and ignore these cues otherwise. In addition to working memory and inhibitory control, task shifting may contribute to differences in performance between incongruent and congruent trials. Third, this inverse correlation is somewhat consistent with a developmental account recently suggested by Piazza, De Feo, Panzeri, and Dehaene (2018), whereby development and education both correlate

with an increased ability to filter our irrelevant cues in incongruent number comparison trials, similar to those in this study. In contrast, performance on congruent trials dropped or remained the same with increased education and age, suggesting there was not a generalized increase in acuity of number perception. Piazza et al.'s developmental findings suggests that better performers on incongruent trials may not benefit as much from congruent visual cues, which may explain this inverse correlation.

Given recent work demonstrating the contribution of numerosity discrimination to math achievement compared to non-numerical bias (Starr et al., 2017), we did expect to see a relation, albeit weaker, between mathematics achievement and accuracy rate on congruent trials. However, in this study, accuracy on congruent trials was unrelated to mathematics achievement, either as a factor distinguishing between achievement groups or as a predictor of mathematics achievement. This was true even before controlling for other academic or cognitive factors. Furthermore, the magnitude of this relation in both analyses was close to zero, showing no trend in the expected direction. This calls into question whether ANS function alone, not measured under high executive function demands, is an important factor related to DD and mathematics achievement more generally. Studies showing no relation between nonsymbolic number comparison performance and math achievement after controlling for executive function have argued this point. For example, in a large sample of TD children, Szűcs, Devine, Soltesz, Nobes, and Gabriel (2014) found that after controlling for other executive function measures such as dot matrices, visuospatial working memory, and the trail-making task, nonsymbolic comparison did not significantly relate to mathematics achievement. Interestingly, in that study, sustained visual attention was the best correlate of ANS acuity, which may further indicate that attention mechanisms and ANS mechanisms are integrally related.

Previous neuroimaging research has shown that congruent and incongruent trials of the nonsymbolic number comparison task recruit different neural mechanisms, with incongruent trials recruiting large portions of the frontoparietal attention network (Leibovich, Vogel, Henik, & Ansari, 2016; Wilkey, Barone, Mazzocco, Vogel, & Price, 2017). Recruitment of additional neurocognitive mechanisms during incongruent trials may be an integral component of the previously assumed direct relation between ANS and mathematics achievement in studies of mathematics learning disability, but also

across the full range of achievement. Supporting this interpretation, recent neuroimaging evidence from Wilkey and Price (in press) shows that individual differences in neural activity of inferior frontal brain regions, indexing the numerical congruency effect in the nonsymbolic comparison task, predicted mathematics achievement in a TD sample of third- and fourth-grade children. This relation held even after controlling for neural activity in a Flanker task and domain-general cognitive factors. In contrast, individual differences in the ratio effect (a neural metric of numerical acuity) did not relate to mathematics, including activity in expected posterior parietal regions. This finding underscores the importance of the neurocognitive mechanisms that interact with magnitude processing mechanisms for mathematics competence, and again speaks to the need to move beyond a single mechanism explanation of foundational competencies for mathematics development.

Limitations and Future Directions

Several factors should be taken into account when interpreting the results of this study. First, participants were recruited from an urban public school system and were mostly from low-income households. Low household income often impedes access to high-quality early mathematics experiences (Ramani & Siegler, 2008), so factors driving the relation between nonsymbolic comparison and mathematics achievement may differ across students with differing household incomes. Furthermore, the relation between nonsymbolic comparison and mathematics achievement in low-income samples has been reportedly lower than middle- and high-income samples (Fuhs, Kelley, O'Rear, & Villano, 2016; Fuhs & McNeil, 2013). However, effect sizes of the relation between nonsymbolic comparison and mathematics achievement from this study are in line with previous meta-analyses (Chen & Li, 2014; Schneider et al., 2017). Additionally, the lack of relation between mathematics achievement and congruent trials, and significant relation between mathematics achievement and incongruent trials, has been previously reported in low-income (Fuhs & McNeil, 2013) and middle-to-high income individuals (Keller & Libertus, 2015). Furthermore, Price and Wilkey (2017) showed that the mediating relation among nonsymbolic comparison accuracy rates and mathematics achievement in the same group of children as this study follows the same patterns as previously reported literature from wider socioeconomic status samples (Lyons & Beilock, 2011).

Second, alternative explanations of the current results are possible. For example, rather than our hypothesis about domain-specific executive function, the current results could indicate that individuals who utilize an appropriate strategy for incongruent trials, whether consciously or not, are better at mathematics. If framed as a task strategy, then strategy selection does not necessarily equate to number-specific executive function. Another alternative is that individual differences in task performance are based not on cognitive efficiencies but rather a predisposition to focus on one aspect of the visual stimuli. A deficit of number-specific executive function is different than the failure to utilize it. Prior research has documented that individuals with a tendency to spontaneously focus on exact quantities have higher arithmetic abilities (Batchelor, Inglis, & Gilmore, 2015; Hannula, Lepola, & Lehtinen, 2010). Recently, this line of research has been expanded to incorporate spontaneous orientation to conflicting or irrelevant dimensions of non-numerical magnitude similar to those of this study (Viarouge et al., 2017). Research on the underlying neurocognitive mechanisms can also help to distill the root of the differences observed in the current results.

A third factor to consider, specifically in regard to the group comparison results, is that choosing to identify a DD group based on consistent, low mathematics achievement over time has both benefits and limitations for interpreting results. In our methods, we make an argument that DD is likely heterogenous in nature and that identifying a "pure dyscalculic" group via the use of an IQ-math achievement discrepancy criteria results in the exclusion of individuals with DD that do not show a discrepancy due to the high comorbidity of other developmental deficits that would affect IQ or another achievement measure such as reading. With this analytic decision comes the limitation that some individuals within the DD group may perform poorly in mathematics testing due to a more globalized cognitive deficit (e.g., IQ) rather than a specific math deficit and, further, that this global deficit was not adequately controlled for when covarying out reading ability and executive function. One solution suggested by Szűcs (2016) may be to focus more on positioning individuals in a multidimensional parametric space that identifies specific cognitive functions related to mathematical performance. The current results suggest that number-specific executive function is likely to be one such cognitive function.

Fourth, this study makes the case that number-specific executive function may be impaired in DD and also related to mathematics achievement across a wide achievement range. This conclusion is based on the idea that a relation between two variables (i.e., math achievement and performance on incongruent trials of the number comparison task) survives after controlling for individual differences in other cognitive factors (i.e., executive function in a non-numerical context). In this type of analysis, the conclusion is only as strong as the validity and specificity of control variables. In this study, only two variables are used as control measures for executive function, and therefore, caution is warranted when considering how completely our variables controlled for all aspects of executive function unrelated to number.

Conclusion

In sum, the two sets of analyses presented here suggest that performance on incongruent trials alone relates to the presence of severe mathematics learning deficits as well as individual differences in mathematics across a wide range of achievement, even when excluding DD individuals. Results suggest that number-specific executive function is a unique predictor of mathematics achievement beyond measures that target the ANS or executive function independently. In order to understand how the intersection of these multiple cognitive mechanisms relates to the acquisition of mathematics skills, future studies should move from a domain-specific versus domain-general approach to experiments that deconstruct this framework. In so doing, future hypotheses can more closely address the integration of cognitive mechanisms required to complete a complex task such as mathematical thought. Furthermore, the current findings do little to explain the relation between nonsymbolic number perception and symbolic number. Understanding their relation may further explain why number-specific executive function relates to symbolic mathematics. This type of investigation may lead to an enhanced understanding of what type of training or remediation of a specific skill set provides the most potential for transfer to improved mathematics achievement more broadly. Given that this study provides support for an integral relation between a "domain-general" mechanism with a number-specific one, a training that seeks to leverage this intersection should be explored.

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Appendix A
Detailed Results From 6.7th Percentile Cutoff Sample Achievement Group Analysis

To make current results more easily comparable to previous literature that used differing cutoff thresholds for determining DD groups, this study also examined whether there were differences between two commonly used thresholds for determining a dyscalculic sample. This threshold has varied widely across studies, and has likely contributed to disagreement among findings (Mazzocco & Myers, 2003). Another commonly used threshold is mathematics achievement scores 1.5 SDs below the nationally normed means, which is equivalent to performance below the 6.7th percentile (Kaufmann et al., 2013; Price et al., 2007; Rotzer et al., 2009). This threshold resulted in the following achievement groupings: DD, ≤ 6.7th percentile; LA, 6.7th–25th percentile; TA, 25th–95th percentile. Again, individuals were placed in achievement groups if their mathematics achievement scores were consistently in the designated achievement range at two of the three early assessments (pre-K–first grade) AND two of the three later assessments (fifth–seventh grades). Given these criteria, 221 children fit into consistent achievement groups across early and later assessment periods, 11 children met the criteria for DD, 22 for LA, and the same 188 children were TA. Descriptive statistics in Table A1.

Results

As in the first achievement group sample, there were no differences according to gender distribution percentages of mathematics achievement groups with the 6.7th percentile cutoff grouping, Pearson $\chi^2(2)$ = 4.045, p = .132, Cramer's V = .132, nor in mathematics achievement, $t(446)$ = 1.182, p = .238, Cohen's d = 0.112, or in nonsymbolic comparison accuracy, $t(446)$ = 0.780, p = .436, Cohen's d = 0.074, at sixth grade, the outcome year of interest for the second set of primary analyses.

Detailed Results From 6.7th Percentile Cutoff Sample Achievement Group Analysis

For the 6.7th percentile cutoff sample, there was an effect of congruency in the DD and TA groups [$t(10)$ = 3.855, p = .003, Cohen's d = 1.968 for DD; $t(187)$ = 6.795, p < .001, Cohen's d = 0.844 for TA], but not in the LA group [$t(21)$ = 0.705, p = .068, Cohen's d = 0.705]. The right panel of Figure A1 shows the congruency effect for DD and TA groups in the 6.7 percentile cutoff sample. Levene's test of equality of variances showed no significant differences in variance across groups for mean accuracy of congruent trials or incongruent trials. Results from the ANOVA showed that there was no effect of achievement group on number comparison performance for congruent trials [$F(2, 218)$ = 0.389, p = .679, η^2 = .003], but there was a significant effect of achievement group on number comparison performance for incongruent trials [$F(2, 218)$ = 4.947, p = .008, η^2 = .043]. After adjusting for multiple comparisons, one-tailed post hoc tests indicated lower accuracy rates for DD than TA children (Bonferroni adjusted p = .003, Hedge's g = 0.997), lower accuracy rates for DD than LA children (Bonferroni adjusted p = .011, Hedge's g = 0.821), and no difference between LA and TA groups (Bonferroni adjusted p = .500, Hedge's g = 0.028).

Results from the ANCOVAs with the covariates of mean accuracy on the Hearts and Flowers mixed trials, max span on the backward Corsi block-tapping test, age at Grade 6 testing, and letter-word identification at the end of kindergarten indicated there was no effect of achievement group on number comparison performance for congruent trials [$F(2, 214)$ = 0.208, p = .812, partial η^2 = .002], but there was a significant effect for incongruent trials [$F(2, 214)$ = 3.356, p = .037, partial η^2 = .030]. After adjusting for multiple comparisons, one-tailed post hoc tests indicated lower accuracy rates for DD than TA children (Bonferroni adjusted p = .034, Hedge's g = 0.895) lower accuracy rates for DD than LA (Bonferroni adjusted p = .017, Hedge's g = 0.893) and no difference between LA and TA groups (Bonferroni adjusted p = .500, Hedge's

Table A1

Descriptive Statistics for Experimental and Standardized Measures

	10th Percentile cutoff sample (*n* = 222, 116 female)			6.7th Percentile cutoff sample (*n* = 221, 115 female)			Entire sample (*n* = 448, 250 female)		
	M	*SD*	Range	*M*	*SD*	Range	*M*	*SD*	Range
Age (years), pre-K	5.1	0.3	4.5–6.4	5.1	0.3	4.5–6.4			
Age (years), sixth grade	12.0	0.3	11.4–13.4	12.0	0.3	11.4–13.4	12.0	.32	11.4–13.4
Nonsymbolic comparison (accuracy, %)	75.5	5.29	58.6–91.4	75.6	5.3	58.6–91.4	74.8	5.48	48.6–91.4
Backward Corsi (max span)[a]	5.1	1.2	2–8	5.2	1.1	2–8	4.81	1.22	2–8
Hearts and flowers (accuracy, %)[a]	76.4	14.4	40–100	76.8	13.9	44–100	73.4	14.5	35–100
Letter-word identification—WCJ–III (K, percentile rank)	111.8	14.1	73–144	111.8	14.2	73–144	109.7	12.7	73–144
Math achievement—WCJ–III (pre-K, percentile rank)	51.3	24.9	1.0–95.0	52.4	23.8	1.0–95.0			
Math achievement—WCJ–III (K, percentile rank)	52.1	24.7	0.0–93.0	52.7	23.8	0.0–93.0			
Math achievement—WCJ–III (first grade, percentile rank)	48.1	24.6	0.4–95.5	48.6	24.1	0.4–95.5			
Math achievement—KM-3 (fifth grade, percentile rank)	39.2	23.5	0.5–96.2	39.6	23.1	0.7–96.2			
Math achievement—KM-3 (sixth grade, percentile rank)	42.1	22.7	0.5–92.5	42.4	22.3	1.0–92.5	27.0	23.1	0.5–92.5
Math achievement—KM-3 (seventh grade, percentile rank)	42.6	22.9	0.5–94.1	42.9	22.5	0.5–94.1			

Note. WCJ–III = Woodcock Johnson–III; KM-3 = KeyMath-3.
[a]Raw scores reported here for year available. See sections 2.4.2 and 2.4.3 for a detailed description of scores used for analyses.
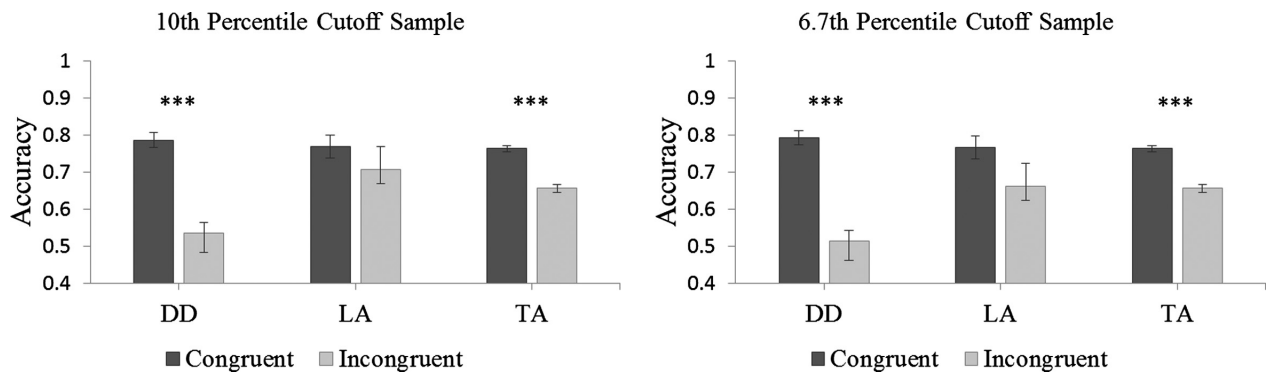

Figure A1. Nonsymbolic number comparison accuracy rates for the sample with developmental dyscalculia (DD) defined as achievement below the 10th percentile (left) and 6.7th percentile (right) split by congruency. LA = low achieving. TA = typically achieving. Error bars represent standard errors. *p*-Values are indicated for differences in accuracy between congruent and incongruent trials (***$p < .001$).

g = 0.112). These results replicate the pattern observed in the ANOVA.

The same ANOVA's and ANCOVAs were conducted on groups formed with the 6.7th percentile cutoff threshold for both congruent and incongruent trials and results fit the same pattern as those of the 10th percentile cutoff. In sum, all ANOVA's and ANCOVAs conducted on both the 10th and 6.7th percentile cut-off samples show the same pattern of results whereby: (a) no group differences are observed for congruent trials of the nonsymbolic comparison task, (b) the DD group performs significantly below LA and TA groups on incongruent trials even when controlling for other cognitive factors and early reading achievement, and (c) no group differences are present between LA and TA groups on incongruent trials.

Appendix B
Details of Missing Sixth-Grade Corsi Span Scores

At the sixth-grade assessment, 22 children (of *n* = 448) did not proceed from instruction in the backward Corsi to successful completion of a trial, indicating noncompliance with the task or a failure

to understand instructions. Scores on outcome measures and covariates of interest for these children were different, on average, from those children who successfully completed the task (nonsymbolic accuracy $t(446) = 3.728$, $p < .001$, Cohen's $d = 0.794$; Hearts and Flowers mean accuracy $t(446) = 3.508$, $p < .001$, Cohen's $d = 0.716$; sixth-grade mathematics achievement $t(446) = 2.587$, $p = .010$, Cohen's $d = 0.613$). Therefore, to avoid nonrandom missing data and include these children in our analyses, backward Corsi max span from the fifth grade was used, where available. To maintain the relative position of children's scores in the fifth grade among other children's sixth-grade scores (fifth-grade mean max span = 4.52, sixth-grade mean span = 4.88), both years of backward Corsi max spans were z-scored and fifth-grade z-scores of the 22 children were used instead of sixth-grade z-scores, which were used for the other 426 children.

Appendix C
Exploration of the Model Fit

In order to better interpret the nonlinear relation between accuracy on incongruent trials of the nonsymbolic number comparison task and mathematics achievement, we plot this relation in Figure 3. This figure shows the fitted relation between untransformed sixth-grade mathematics achievement and nonsymbolic number comparison accuracy on incongruent trials for Model M6, holding Hearts and Flowers accuracy, backward Corsi span, early reading achievement, and age at testing in sixth grade at their sample means. As Figure 3 shows, the magnitude of the relation between accuracy on incongruent trials and mathematics achievement is greater for students with higher accuracy, on average. For example, the estimated difference between students with 30% and 40% accuracy on nonsymbolic number comparison is associated with a difference of 1.0 percentile rank points in sixth-grade mathematics achievement, on average. The difference between students with 75% and 85% accuracy
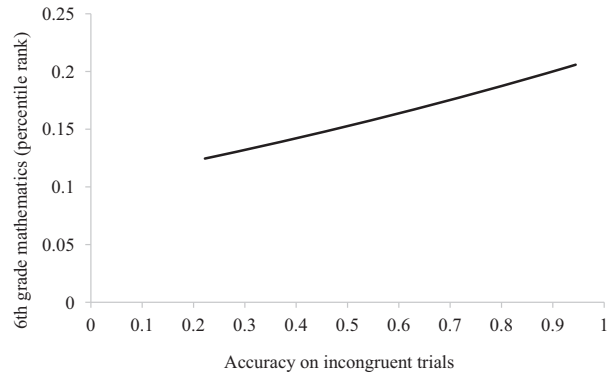

Figure B1. Predicted sixth-grade mathematics achievement as a function of accuracy on incongruent trials of nonsymbolic number comparison, for students with average domain-general executive functioning and early reading achievement, and of average age at testing in sixth grade.

on nonsymbolic number comparison is associated with a difference of 1.3 percentile rank points in sixth-grade mathematics achievement, on average.

Supporting Information

Additional supporting information may be found in the online version of this article at the publisher's website:

Figure S1. Scatter Plots of Nonsymbolic Number Comparison Performance Measures and Composite Math Achievement (A, B, C) and a Plot of Congruent by Incongruent Accuracy Rates (D)

Table S1. Descriptive Statistics for Experimental and Standardized Measures

Table S2. Task Details for Number Comparison Tasks of All Formats, $n = 448$

Table S3. Pearson r Values for Bivariate Correlations Between Measures Included in Regression Model Predicting Sixth-Grade Mathematics Achievement

Table S4. Comparison of Nonsymbolic Comparison Performance and Keymath-3 Subtest Correlations